FIRE RESISTANCE OF CONCRETE STRUCTURES

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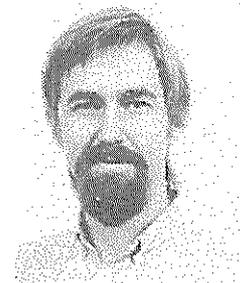
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ABSTRACT

A prediction of structural behaviour and fire resistance is pre-
sented for some different types of concrete members. This is
made by use of two computer programs TASEF-2 and CONFIRE for
thermal and structural response, respectively.

Fire resistance times predicted by CONFIRE for different failure
criteria and those obtained from different design recommenda-
tions are compared for a simply supported plate strip.

The influence of axial restraint calculated by CONFIRE and by
use of the PCI-manual are compared.

Two column tests are also analysed successfully with the pro-
gram.

This paper is a result of a commenced co-operation in
the structural fire engineering research between Lund Institute
of Technology and SINTEF. Improved design methods and a more use-
ful code is an important goal of the co-operation.

1.   MATERIAL BEHAVIOUR MODELLING

1.1   Concrete

When modelling material mechanical behaviour, an analytical de-
scription is required of the relationship between stresses and
strains. A computer oriented constitutive model for concrete in
compression, valid at transient high temperature conditions, was
presented in Anderberg & Thelandersson 1976 /1/ and is used here
in the structural program CONFIRE /2/. The model is based on the
concept that the total strain ε can be separated into four com-
ponents

$$\varepsilon = \varepsilon_{th}(T) + \varepsilon_{\sigma}(\bar{\sigma},\sigma,T) + \varepsilon_{cr}(\sigma,T,t) + \varepsilon_{tr}(\sigma,T) \tag{1}$$

where

ε_{th} = __thermal strain__, including shrinkage, measured on specimens under variable temperature

ε_{σ} = instantaneous, __stress-related strain__, based on stress-strain relations obtained under constant, stabilized temperature

ε_{cr} = <u>creep strain</u> or time-dependent strain measured under constant, stabilized temperature .

ε_{tr} = <u>transient strain</u>, accounting for the effect of temperature increase under stress, derived from tests under constant stress and variable temperature

σ = stress

$\bar{\sigma}$ = stress history

T = temperature

t = time

The order of importance for the strain components can be studied from Fig 1 which is based on a curve representing a transient test with a load level of 35% of inital ultimate load. The predominance of the transient strain is obvious.

A complete description of the model is given in Anderberg & Thelandersson /1/.
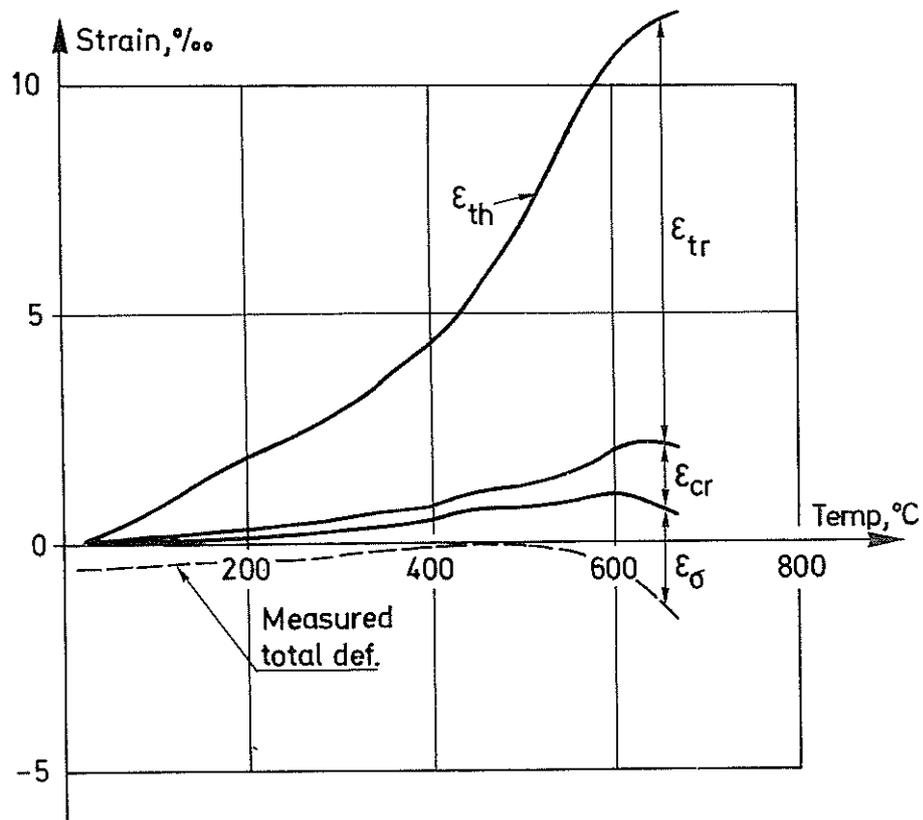
Fig 1   Relation between different strain components as calculated by the material model for a transient test at a load level of 35% of ultimate load at ambient conditions

1.2   Steel

It is generally agreed that the deformation process of steel at transient high temperatures can be described by three strain components defined by the constitutive equation

$$\varepsilon = \varepsilon_{th}(T) + \varepsilon_{\sigma}(\sigma,T) + \varepsilon_{cr}(\sigma,T,t) \tag{2}$$

where

ε_{th} = thermal strain

ε_{σ} = instantaneous, stress-related strain based on stress-strain relations obtained under constant, stabilized temperature

ε_{cr} = creep strain or time dependent strain

A computer oriented mechanical behaviour model for steel, based on Eq. 2, is developed in Anderberg /3/ and applied in CONFIRE.

2.   COMPUTER PROGRAMS

Two computer programs, based on the Finite Element Method, are employed in the numerical examples presented in the subsequent sections:

-       TASEF-2 by Wickström /4/ for the nonlinear transient heat flow analysis,

-       CONFIRE by Forsén /2/ for the nonlinear analysis of concrete frames subjected to fire.

TASEF-2 is developed from the Fourier heat balance equation in matrix form for a two dimensional field. Rectangular and/or triangular elements may be employed. The temperature dependent conductivity coefficient and specific volumetric enthalpy are given as input. Estimates of these parameters are given in the literature and are dependent on the moisture content, aggregate type etc; cf. Wickström /4/, Schneider /5/, Thelandersson /6/ and Anderberg /3/.

An arbitrary external temperature-time curve, which may be defined by the user, simulates the fire exposure. The temperature distribution within the structure at prescribed times are obtained by use of an explicit forward integration method.

CONFIRE is developed from the computer program CONFRAME by Åldstedt /7/. A beam element with 3 degrees of freedom (DOF) at each node and one internal axial DOF is employed. The total strain ε over the cross-section of the element is taken as linear (Bernoulli-Navier). The temperature related material behaviour models for steel and concrete defined in section 1 are incorporated. Thus, nonlinear material properties are accounted for, including temperature dependent stress-strain relationship, creep, thermal strain and transient state concrete strain. Non-

linear geometric effects may also be accounted for. The linear element tangent stiffness matrixes and the element stress resultant vectors are obtained by Gaussian integration with fixed integration points. The geometric element stiffness matrix is obtained by analytical integration. The time dependent stresses, strains and structural displacements are obtained step by step by use of the Newton-Raphson iteration method, solving the linearized incremental system equilibrium equation. The current temperature distributions are recorded at each step from a temperature file.

Fig 2 shows the main composition of the whole unit established for the computer analysis.
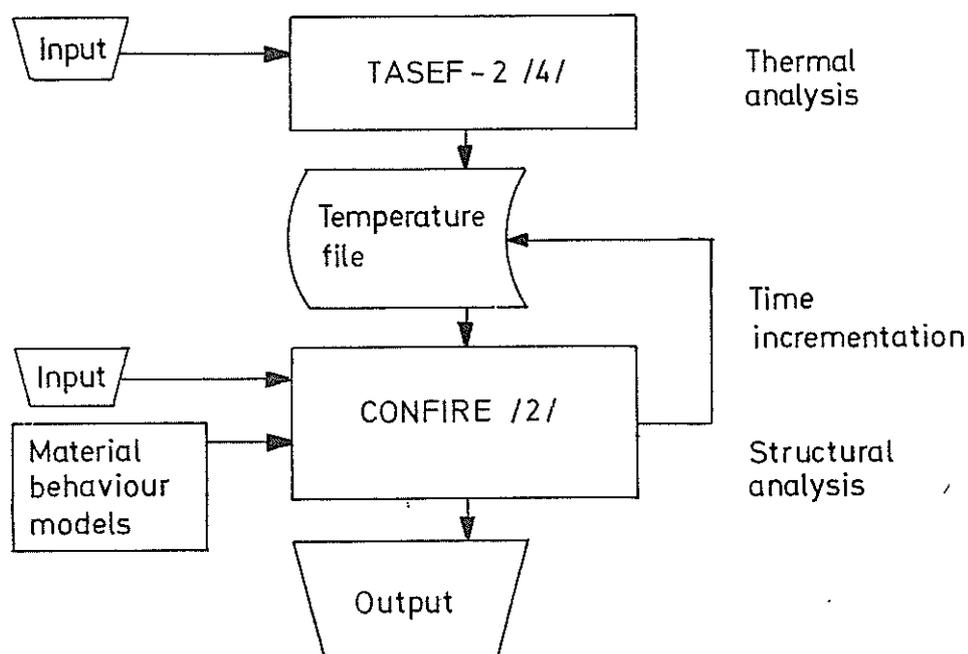
Fig 2   Main composition of the computer analysis

3.   SIMPLY SUPPORTED PLATE STRIPS

The structural response of a simply supported, fire exposed plate strip is predicted by use of TASEF-2 /4/ and CONFIRE /2/; cf. section 2. The fire exposure is given by the standard temperature-time curve according to the ISO 834 fire resistance test. Three different cases are considered, see Fig 3

- Case 1 : Reinforced plate strip, twin load 13.8 kN (65% of initial ultimate load)

- Case P1: Prestressed plate strip, twin load 13.8 kN (65% of initial ultimate load and initial prestressing strain = 5‰)

- Case P2: Prestressed plate strip, twin load 10 kN (full pre-
         stressing at the time t = 0 and initial prestressing
         strain = 5‰)

$$A_s = 391 \text{ mm}^2 \quad A_s^P = \frac{450}{1450} \cdot 391 = 121 \text{ mm}^2$$
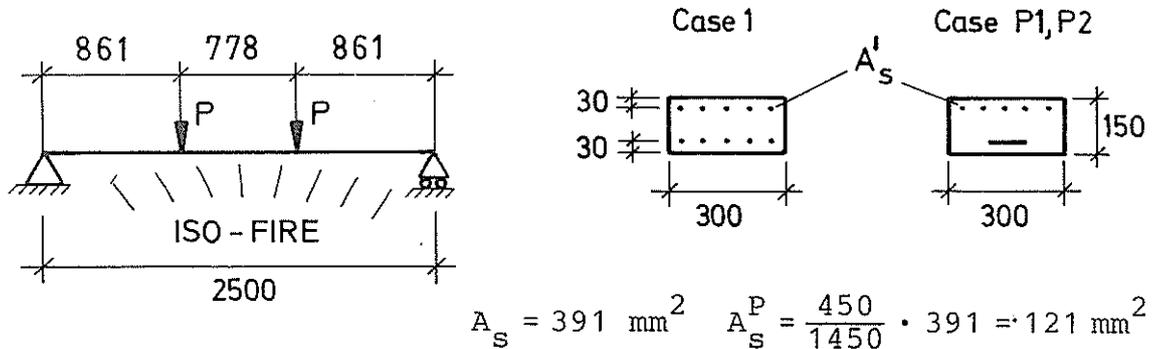
$f_{cc} = 20$ MPa   Case 1 : P = 13.8 kN = 0.65 P_{ult}

$f_{0.2} = 450$ MPa   Case P1 : P = 13.8 kN, $\varepsilon_s^P = 5‰$

$F_{0.2}^P = 1450$ MPa   Case P2 : P = 10.0 kN, $\varepsilon_s^P = 5‰$

ε_s^P = prestressing strain, A_s^P = prestressing steel area

Fig 3   Characteristic data for three test examples, Case 1, P1
         and P2

The initial moisture content in the concrete is taken as 3% by
weight. The resulting emissivity at the concrete surfaces is set
to 0.8, and the convection heat transfer coefficient is taken as
25W/m²°C. Material properties according to Anderberg /3/ and
Harmathy & Stanzak /8/ are assumed for the hot-rolled, reinforc-
ing steel and the cold-drawn, prestressing steel ASTM A421, re-
spectively. Note that the prestressing steel type ASTM A421 is
non-stabilized. At present, relevant creep data for the more
commonly used stabilized prestressing steel types have not yet
been obtained.

The predicted structural response of the plate strip in Case 1,
P1 and P2 is shown in Fig 4 in terms of mid-span deflection and
stress in tensile reinforcement and prestressing steel, respec-
tively. Correspondingly, Fig 5 gives the concrete stresses over
the mid-span cross-section for all three cases. Table 1 shows
different values of the fire resistance, t_f, obtained from the
analysis for the cases 1, P1 and P2. As indicated in the table,
four different failure criteria are employed:

–   max deflection $\delta = L/30$ (L = span length)

–   max deflection rate $\frac{\Delta L}{\Delta t} = L^2/9000h$ (h = height of cross-
                                                              section)

–   max concrete strain (at approx. 50°C) $\varepsilon_\sigma = 7‰$

–   max steel strain $\varepsilon_\sigma = 20‰$

Further, different values of t_f obtained in design recommenda-
tions from Refs /9/, /10/, /11/ and /12/ are included in Table 1.
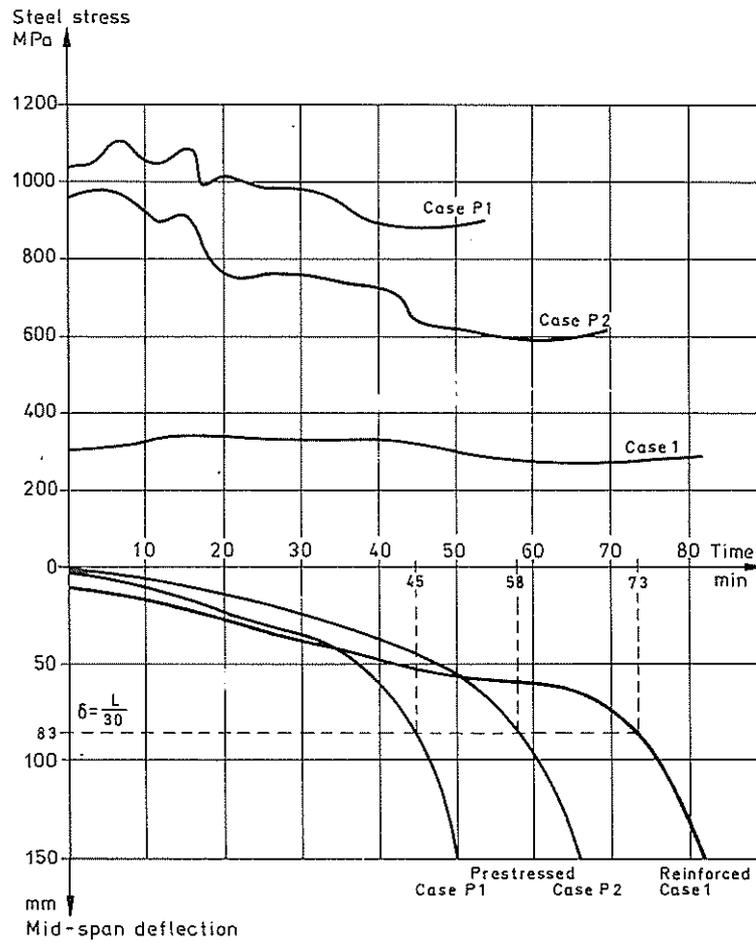
Fig 4   Predicted structural behaviour of a fire-exposed plate
         strip in terms of mid-span deflection and steel stress.
         Data for the calculation are given in Fig 3
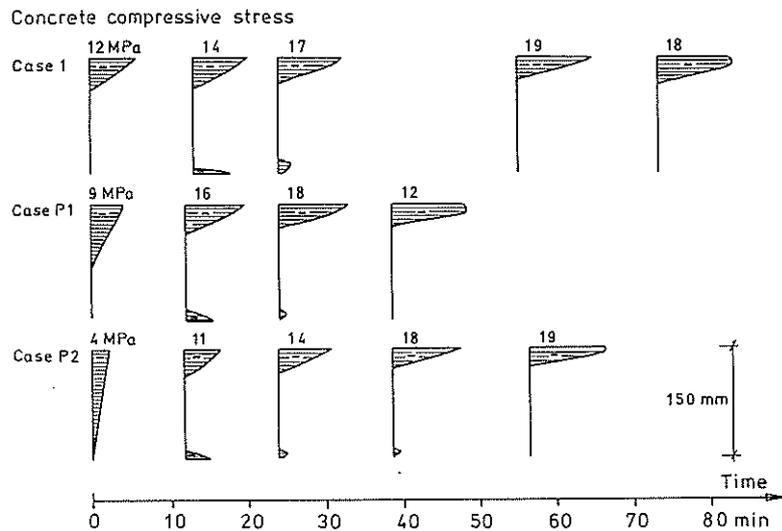
Fig 5   Predicted concrete stresses for the three cases 1, P1
         and P2. Data for the calculation are given in Fig 3

Table 1   Different values of the fire resistance in minutes obtained for Case 1 (reinforced) and cases P1 and P2 (prestressed).

*Temperature distributions obtained by TASEF-2 /4/

Case	Present analysis. Failure criterion:				Design recommendations				
	$\delta \geq L/30$	$\dfrac{\Delta\delta}{\Delta t} \geq \dfrac{L^2}{9000h}$	$\varepsilon^c_\sigma \geq 7\,°/_{\infty}$	$\varepsilon^s_\sigma \geq 20\,°/_{\infty}$	NS 3478 /9/	PCI /10/	CEB /11/	CEB /11/ *mod.temp.	Swedish manual /12/
1	73	72	<u>82</u>	<u>82</u>	75	102	90	82	—
P1	45	41	<u>50</u>	—	40	55	—	—	50
P2	58	56	<u>67</u>	—	—	75	—	—	60

Note that a failure criterion based on strain limits (underlined in Table 1) is more consistant with the present analysis than failure criteria based on deflections/deflection rates. The latter criteria have been developed for standard fire resistance tests.

For the cases P1 and P2, the strain limit for concrete (7‰) is attained at a time, when the stress-related strain in the prestressing steel is only about 6‰ (creep excluded). This is due to the very high creep in prestressing steel (about 20‰ just before concrete strain limit is exceeded) which causes the failure.

The fire resistance times in Table 1, obtained from NS 3478, are based on table values. The fire resistance times obtained from Refs. /10/, /11/ and /12/ are the result of tensile stress calculations at failure ($t = t_f$). The tensile steel stress combined with the different "steel stress - critical temperature" curves and data for the temperature development, which are presented in these references, determine the fire resistance time in each case.

Clearly, the fire resistance times obtained from PCI /10/ are significantly higher than those obtained from the other sources /9/, /11/ and /12/. This is due to the fact that both the mechanical properties of steel and the temperature development in concrete (silicious) are estimated less conservatively in PCI /10/ than in Refs. /9/, /11/ and /12/.

For the case P1 (prestressed), the common interpretation of the Norwegian Code NS 3478 /9/ - which is employed here - is believed to be too conservative.

Note that, likely, somewhat higher fire resistance times in the cases P1 and P2 would have been obtained from the analysis if stabilized prestressing steel had been employed rather than the non-stabilized prestressing steel ASTM A421. However, as indicated previously, relevant creep data are at present available only for ASTM 421.

4.   INFLUENCE OF AXIAL RESTRAINT

It has been shown in tests on axially restrained, reinforced slabs and beams /14/ that great axial forces may sometimes develop. Such axial restraint forces may increase the fire endurance significantly /10/. It is therefore of principal interest to investigate if the thermal thrust, T, generally can be utilized in a fire design.

In the PCI-manual "Design for fire resistance of precast pre-stressed concrete", a calculation procedure is developed for determining the thermal thrust. The calculation is based on tests on a double T-unit of normal weight concrete and lightweight concrete. In the tests each specimen was permitted to expand to a given amount and further expansion was prevented. After expansion was stopped, the restraining force increased to a maximum value and then either diminished or remained relatively constant. Fig 6 illustrates the maximum measured restraining forces for the pre-

Reference specimen
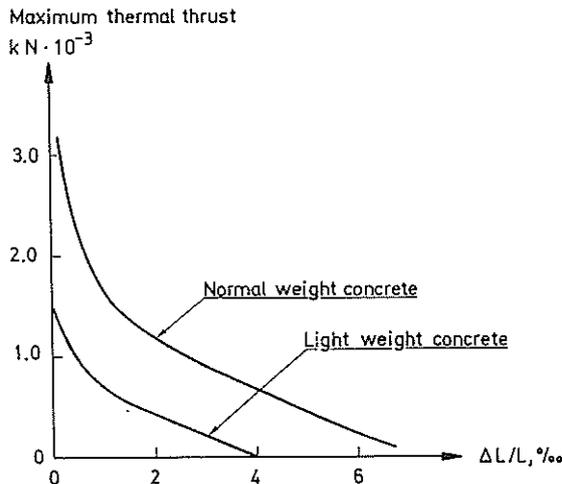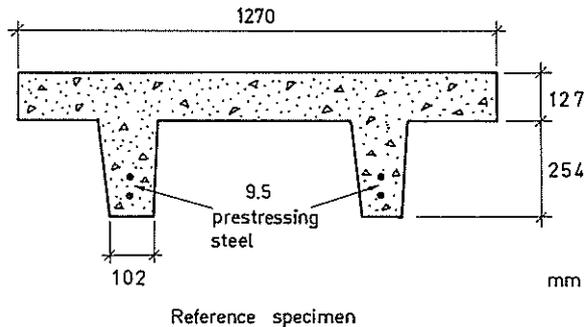
Fig 6   Maximum restraining force measured during tests of reference specimens /10/

stressed specimens. It is significant that a small increase in expansion is accompanied by a large reduction in the restraining force. In the PCI-manual, nomograms are developed by extrapolation of test results for determining the thermal thrust for any given reinforced or prestressed cross-section. Entrance parameters are strain parameter ΔL/L and ratio of cross-sectional area to heated perimeter A/s. This nomogram is here applied on the fire-exposed plate strip examined in section 3.

The behaviour of the plate strip is predicted by CONFIRE for different permissible expansions ΔL = 0, 2, 4 and 6 mm at the center of gravity. The development of the axial force during a thermal exposure according to the ISO 834 standard fire resistance test is illustrated in Fig 7. The second order effects are included in
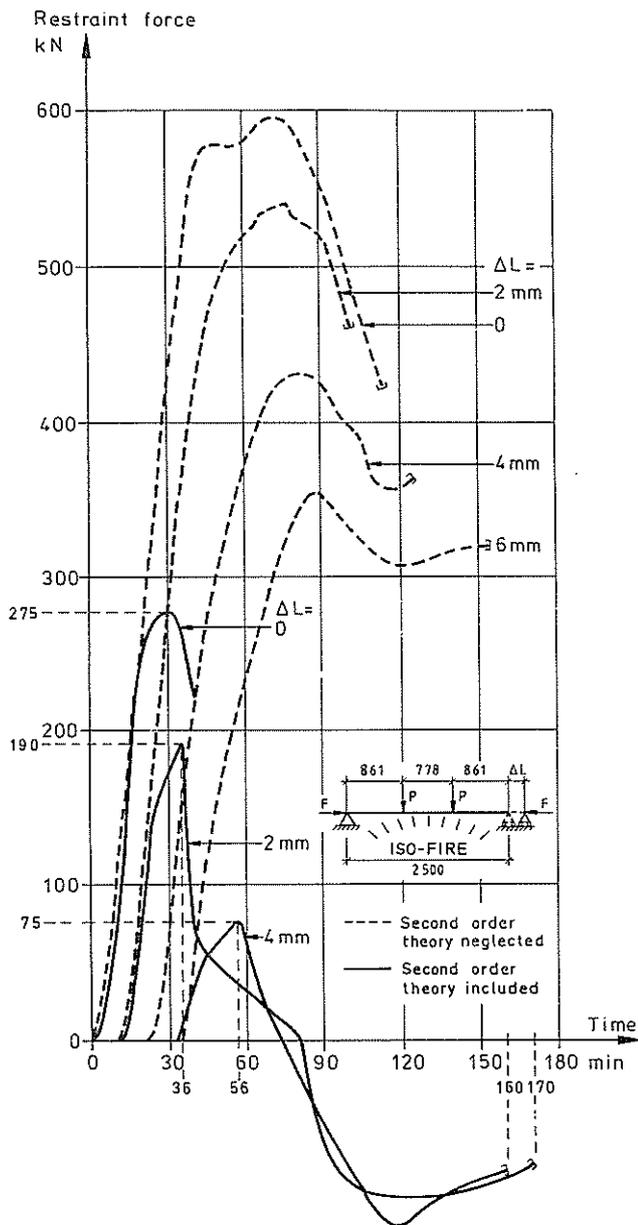
Fig 7   Restraint forces for a fire-exposed, reinforced plate strip (Case 1, as shown in Fig 3) at different permissible expansions ΔL/L = 0, 2, 4 and 6 mm and thereafter a complete restraint. Center of gravity is the point of action for restraint forces

the full line curves but not in the dashed curves. The calulation illustrates the necessity to include the second order theory in the calculation. The full line curves, case a, b and c, illustrates a structural behaviour which has not been possible to derive earlier. The thermal thrust attains a maximum value at an early stage, after the thrust has started to develop, and it then decreases rapidly and transfers into tension, if membrane forces can be taken at supports. If membrane action is not possible, failure occurs when the thermal thrust has diminished to zero or possibly somewhat later. Table 2 illustrates characteristic data from the calculations.

Table 2   Characteristic results from CONFIRE calculations of an axially restrained, reinforced plate strip (Fig 3) at different permissible expansions

	Permissible expansion ΔL mm	Max thermal thrust		Failure time		Max deflection mm
		kN	Time min	No membrane action min	Membrane action min	
a	0	281	30	–	–	
b	2	190	36	≥82*	170	185
c	4	75	56	≥73*	160	175
d	6	0	–	–	–	

*These failure times are related to the time when the thermal thrust transfers into tension force and therefore the simply supported plate strip may fail somewhat later.

The table shows for all cases that without membrane action the failure time is much greater than the time at which maximum thrust occurs. This means that the maximum thrust for the plate strip studied cannot be utilized when calculating the fire resistance according to the PCI-manual. The table also shows the great deflections occurring during membrane action. It must be emphasized that the development of restraint forces are very sensitive to the point of action of the cross-section.

If the maximum thermal thrust is calculated in accordance with PCI-manual the curve shown in Fig 8 is obtained. In the same figure the results are also given for the CONFIRE calculation. The difference between the curves is very obvious for $\Delta L/L > 0.15\%$. The conclusion from the analytical study is that the maximum thrust, acting at center of gravity, is smaller than according to the PCI-manual and at failure state, there is no longer any thrust.

The study illustrated here indicates that even if axial forces develop they may have no significant positive effect on the fire resistance. The point of action also ought to be considered. The PCI-

calculation method, therefore, cannot be adopted generally. It
can also be discussed if such a free elongation ΔL/L, followed
by a complete restraint, occurs in "real life". It should be more
realistic to simulate different degrees of restraint defined by
actual axial stiffness when studying thermal thrust.
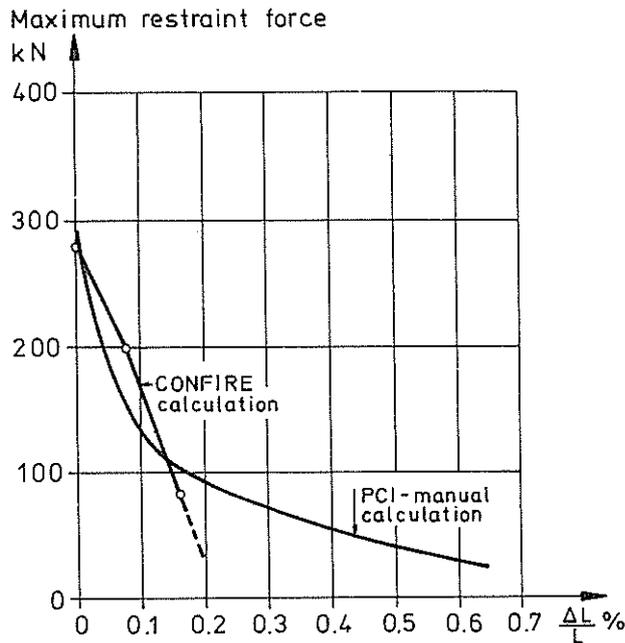
Fig 8   Maximum restraining force as a function of permissible
          expansion ΔL/L for Case 1 (see Fig 3). A comparison bet-
          ween CONFIRE prediction and PCI-manual design calcula-
          tion

5.   STRUCTURAL RESPONSE OF FIRE-EXPOSED COLUMNS

The program CONFIRE has also been used for verifying its reli-
ability on two reinforced concrete columns exposed on three sides
to ISO 834 standard fire and tested at the Swedish National Test-
ing Institute in Borås. A similar theoretical study has been made
in /15/. The principal testing arrangement is illustrated in Fig
9 which shows the concrete column placed at the vertical furnace
opening (b·l·h = 3·1.8·3 m³). The hydraulic loading is applied
either centrically or eccentrically, as illustrated in Fig 9.
The column is heated on three sides according to ISO 834 and
lightweight concrete walls close the furnace. Material data of
the column used in the calculation are as follows:

Moisture content $u = 6\%$ by weight

Reinforcement Ks 40 Ø16 $f_{0.2} = 450$ MPa

                                    $f_u = 716$ MPa

Silicious concrete $f_{cc} = 34$ MPa

    Thermal conductivity   reference /3/
    and enthalpy

The load bearing capacity at room temperature for an eccentrici-
ty of 6 cm was determined by testing to 0.95 MN.
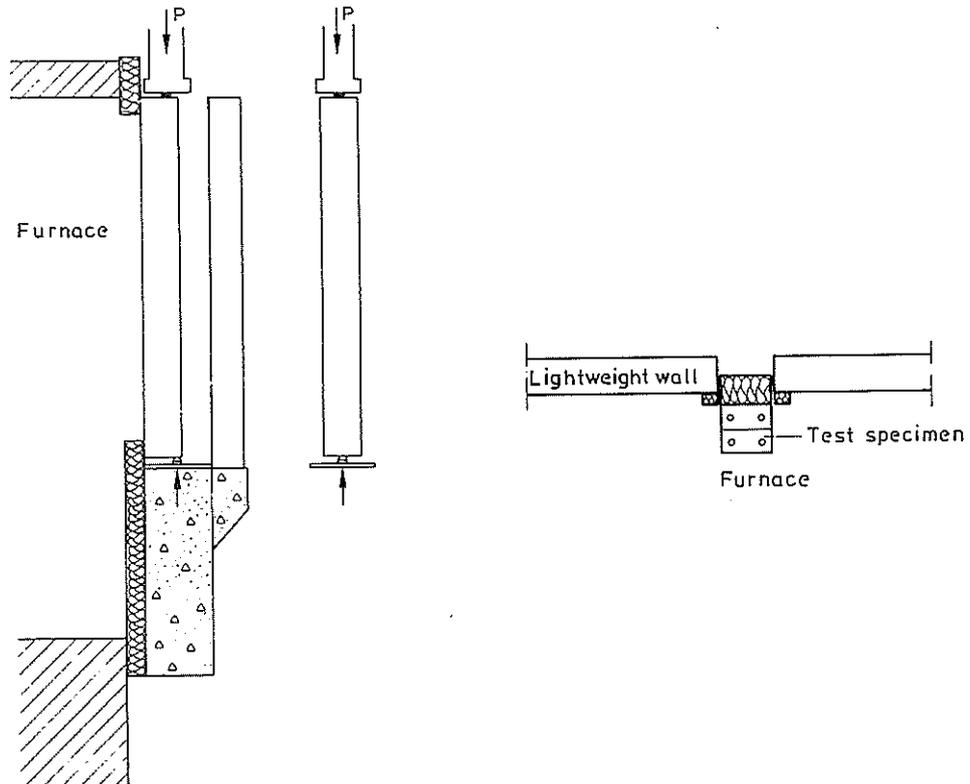
<u>Fig 9</u>   Testing arrangement

5.1   Results

The predicted and measured temperatures are illustrated in Fig
10. This figure gives the temperature of six points at the mid-
section of the column as a function of time. The very good agree-
ment obtained with TASEF-2 is significant and is earlier docu-
mented in /15/. Predicted temperatures are then inserted into
CONFIRE structural program.

In the first study, the column is loaded to 0.6 MN with an eccen-
tricity of 6 cm, directed from the furnace. The load corresponds
to 63% of the ultimate load at normal conditions. In the test the
measurements were stopped after 0.5 h due to a support failure,
which was a mishap, but a comparison is still of interest. Fig
11 illustrates mid-points deflection and axial elongation as a
function of time obtained in test and calculation. The predicted
deflection v, directed towards the furnace is in a very good a-
greement with the test but the axial elongation differs somewhat.
The predicted and test estimated fire resistance are both about
0.7 h.

In the second comparison the same column was loaded to 0.3 MN
with the same eccentricity but directed towards the furnace (see
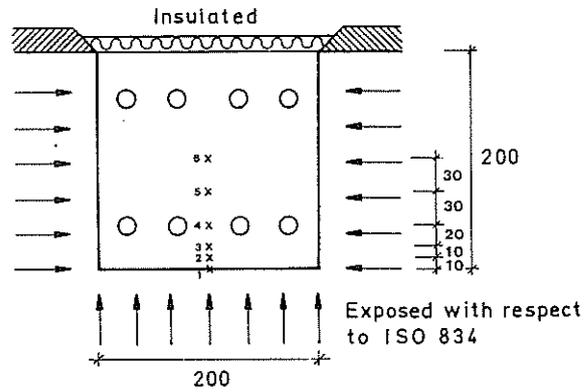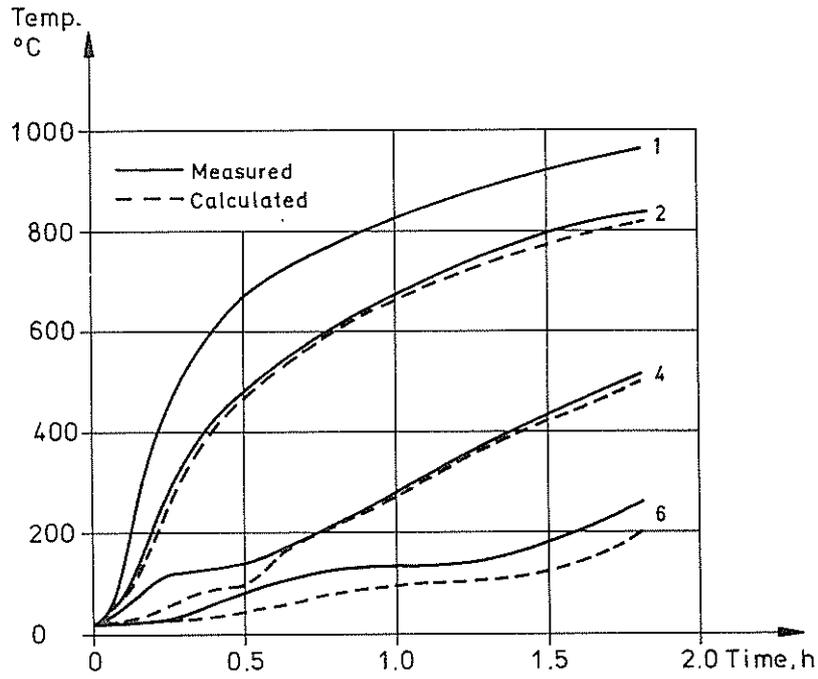
Fig 10   Measured and calculated temperatures in the mid-section of the column

Positive v : Deflection towards fire
Positive Δ : Expansion
———————— Experiment
— — — — — Present analysis
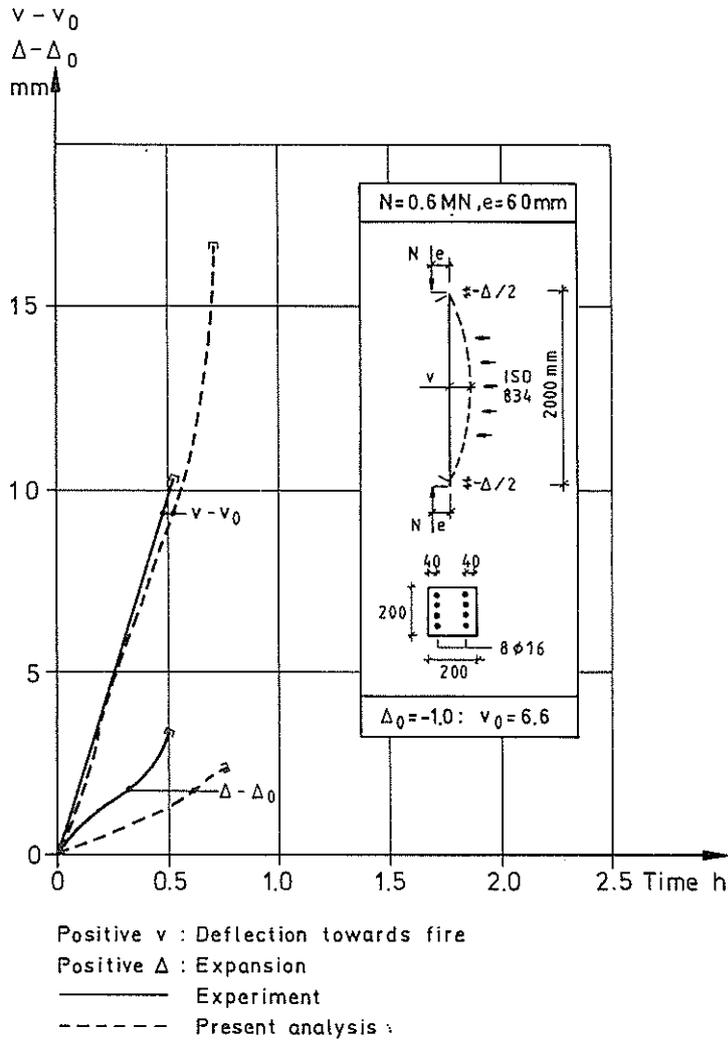
Fig 11   Measured and calculated behaviour of a reinforced con-
          crete column in a fire, eccentrically loaded to 0.6 MN

Fig 12). This load corresponds to 31% of the original ultimate
load. Both the predicted mid-point deflection, the axial move-
ment and failure time are in a quite good agreement with measured
behaviour as shown in Fig 12. It can be noted that the column ex-
panded axially both in calculation and experiment during the
first 1.7 h, but then it transferred into contraction in experi-
ment. The sudden change into failure state is caused by a rapid
inwards movement of the compression zone into the cross-section,
which means that the tensile stress in the reinforcement in-
creases to a critical value.

The two examples illustrate the reliability of TASEF-2 and
CONFIRE computer programs.
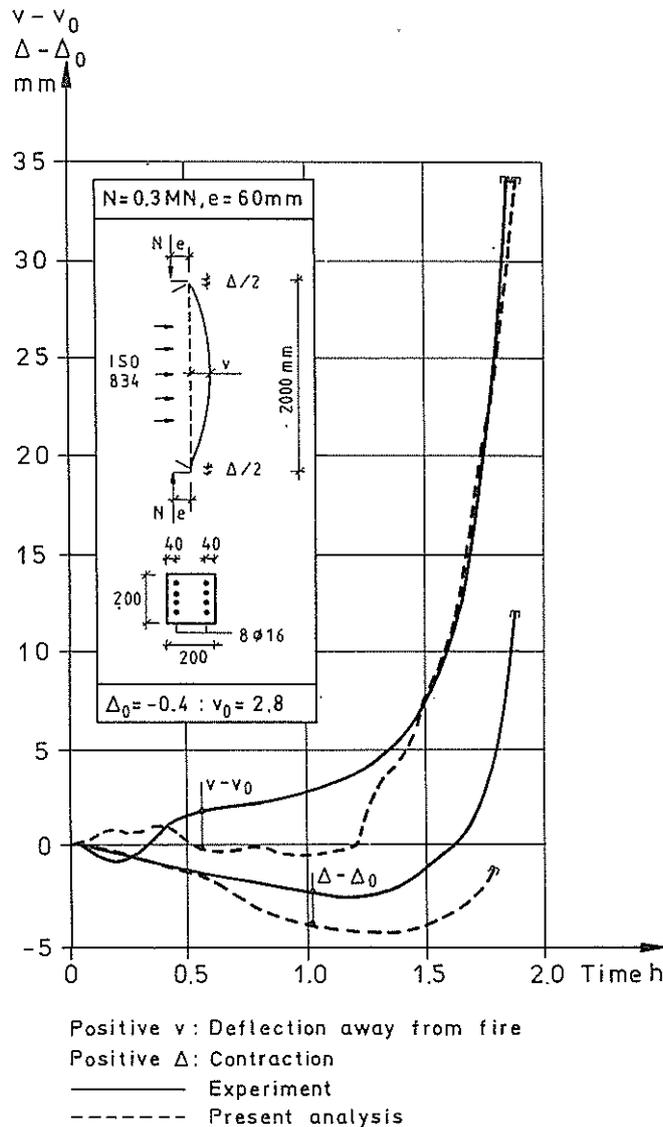
Fig 12   Measured and calculated behaviour of a reinforced con-
          crete column in a fire, eccentrically loaded to 0.3 MN

6.   CONCLUSIONS

Presented results illustrate the capability and reliability of
TASEF-2 temperature program and CONFIRE structural program deve-
loped at LTH and NTH, respectively. Decisive for the results are
the behaviour models at elevated temperatures of concrete and
steel developed at LTH. The paper fragmentarily shows that cur-
rent design recommendations in respect to fire sometimes seem to
be based on too rough estimates or to be too generalized. This is
due to the fact that the complicated behaviour of fire exposed
concrete structures has not yet been understood that well. How-
ever, the tool has now been further developed for analyzing most
common structures.

Such computer calculations can now give basis for improving the
design methods and to build up a much more useful and efficient
code. This mode of activity has already started within the work
of a Swedish Manual /12/ but may now be intensified in all Nor-
dic countries as a co-operation project.

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